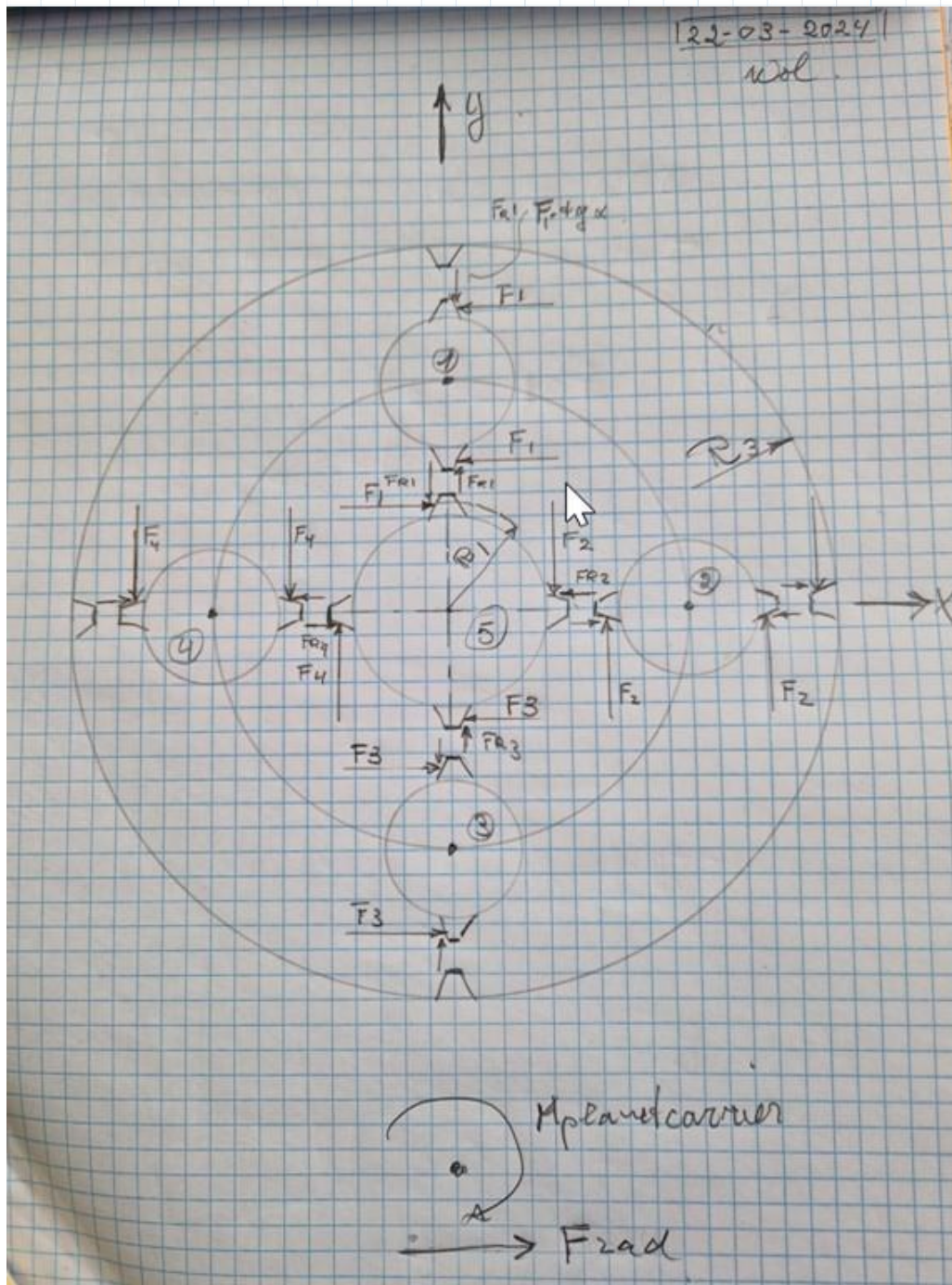## Gear ring forces

The purpose of this spreadsheet is to calculate the forces between
the sunwheel and the planet gears. The geometry of the tooth profile
is not considered. The problem here is that we have 3 equations and
4 unknowns. Often, these equations are solved by addressing the
geometry issue.

Pitch diameter of the gear ring	$D_{gearring} := 1.2 \; m$	$R_{gearring} := \dfrac{D_{gearring}}{2}$
Pitch diameter of the pinion	$D_{pinion} := 0.3 \; m$	$R_{pinion} := \dfrac{D_{pinion}}{2}$
Moment planet carrier	$M_{pl} := 2500 \; kN \cdot m$	
Pressure angle	$\alpha_1 := 20 \; deg$	

Averge tooth load

Force of on the planet carrier divided over 4 planet wheels

$$F_{pl} := \frac{M_{pl}}{R_{gearring} \cdot 4} \qquad\qquad F_{pl} = 1041.667 \; kN$$

Radial load on the planet carrier $\qquad F_{rad} := 290 \; kN$

The radial load on the tooth of the sun wheel

Add. load on planet 1 $\qquad\qquad F_1 := 122 \; kN$

Add. load on planet 2 $\qquad\qquad F_2 := -40 \; kN$

Add. load on planet 3 $\qquad\qquad F_3 := -134 \; kN$

Add. load on planet 4 $\qquad\qquad F_4 := 53 \; kN$

Force with added load 1 $\qquad F_{1n} := F_1 + F_{pl} \qquad F_{1n} = \left(1.164 \cdot 10^3\right) \; kN$

Force with added load 2 $\qquad F_{2n} := F_2 + F_{pl} \qquad F_{2n} = \left(1.002 \cdot 10^3\right) \; kN$

Force with added load 3 $\qquad F_{3n} := F_3 + F_{pl} \qquad F_{3n} = 907.667 \; kN$

Force with added load 4 $\qquad F_{4n} := F_4 + F_{pl} \qquad F_{4n} = \left(1.095 \cdot 10^3\right) \; kN$

$$F_{avx} := \frac{\left(F_{1n} + F_{2n} + F_{3n} + F_{4n}\right)}{4} \qquad\qquad F_{avx} = 1041.917 \; kN$$

Setup first equations of motion

We now have three equations: the moment balance and force balances in the x and y directions. To solve this system, we need four equations. However, the moment balance provides only one additional equation.

To obtain the fourth equation, we can leverage the geometric symmetry of the gear system. We can assume that the forces are evenly distributed across the planetary gears, and that the radial load is equal on each tooth. With this geometric assumption, we can derive a fourth equation.

By solving these four equations, we can determine the forces on the teeth of the gear system and thereby solve the problem.

The three equations

Moment balance around the axis of the planetary carrier:
The moment balance around the axis of the planetary carrier tells us that the sum of all moments around this axis must be equal to the total moment on the planetary carrier. So:

M_pl = (F_1 + F_2 + F_3 + F_4) × (2/3)

Here:

M_pl = 2500 kNm, the moment on the planetary carrier.
D = 1.2 m, the diameter of the gear ring.
F_1, F_2, F_3, F_4 are the unknown forces on the teeth of the gear system.

Force balance in the x-direction:

F_1 − F_2 × tan(α) − F_3 + F_4 × tan(α) = Frad

Here, Frad = 290 kN is the radial load on the planetary carrier. See the freebody diamgram

Force balance in the y-direction:

− F_1 × tan(α) − F_2 + F_3 × tan(α) + F_4 = 0

Force wit

Force wit

Force wit

Force wit

$F_{avp} := \dfrac{(F}{}$

$F_{add} := (F$

Step 1: Adding extra geometric symmetry for uniform force distribution

We utilize the geometric symmetry of the gear system by assuming that the forces are evenly distributed across the planetary gears, and that the radial load is equal on each tooth. Thus, each tooth experiences

Fr = (F1 + F2 + F3 + F4) / 4 Fr

Fr is used to indicate the even distribution of force across the four teeth of the planet carrier. This force is the sum of all forces on the teeth divided by the number of teeth, and is used to check if the forces are evenly distributed across the teeth. F1, F2, F3, and F4 are the forces on the planet gears.

4 Equations assumming that that the forces are evenly distributed across the planetary gears

Moment balance around the axis of the planetary carrier:

M_pl = (F_1 + F_2 + F_3 + F_4) × (2D/3)

Here, M_pl = 2500 kNm is the moment on the planetary carrier, and D = 1.2 m is the diameter of the gear ring.

Equation for uniform force distribution:

Fr = (F_1 + F_2 + F_3 + F_4) / 4

Here, Fr is the radial force evenly distributed over each tooth.

Force balance in the x-direction:

F_1 − F_2 × tan(α) − F_3 + F_4 × tan(α) = Frad

Here, Frad = 290 kN is the radial load on the planetary carrier.

Force balance in the y-direction:

− F_1 × tan(α) − F_2 + F_3 × tan(α) + F_4 = 0

With these four equations, we have established a system of equations describing the forces on the teeth of the gear system. We can now use numerical methods to solve this system and find the values of F_1, F_2, F_3, F_4.

Solving the forces F1,F2, F3 and F4

The coefficient matrix A and the right-hand vector b are formed as follows:

coefficient matrix A

$$A := \begin{bmatrix} 1 & 1 & 1 & 1 \\ \dfrac{1}{4} & \dfrac{1}{4} & \dfrac{1}{4} & \dfrac{1}{4} \\ 1 & -\tan\left(\alpha_1\right) & -1 & \tan\left(\alpha_1\right) \\ -\tan\left(\alpha_1\right) & -1 & \tan\left(\alpha_1\right) & 1 \end{bmatrix}$$

vector matrix

$$b := \begin{bmatrix} \dfrac{2 \cdot M_{pl}}{D_{gearring}} \\ F_{avx} \\ F_{rad} \\ 0 \end{bmatrix}$$

Found a singularity whil eluvating this expression. You may divide by 0 or inverting a singularity matrix

$$bb := \lVert A \rVert \qquad bb = 0$$

$$Inv := \boxed{A^{-1}}$$

$$xx := \boxed{A_{coeff}}^{-1} \cdot b$$