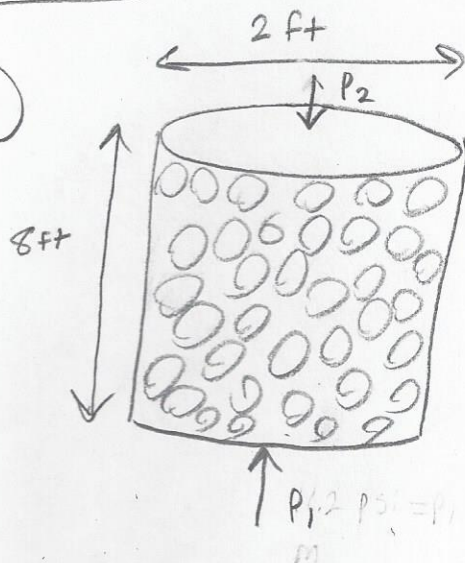


HW 4

①



$$T = 100^\circ\text{F}$$

$$D_p = 0.5''$$

$$\varepsilon = 0.38$$

$$\dot{m} = 47.5 \text{ lbm/min}$$

$$\Delta P = ?$$

$$P_1 = 16.2 \text{ psia}$$

$$\beta = ?$$

$$\mu = 4.02 \times 10^{-7} \frac{\text{slug}}{\text{ft}\cdot\text{s}} \times \frac{32.2 \text{ lbm}}{\text{slug}} = 1.29 \times 10^{-5} \frac{\text{lbm}}{\text{ft}\cdot\text{s}}$$

$$\rho_{\text{air}} = \frac{RT}{P}$$

$$\beta = \frac{PM}{RT}$$

$$\phi_s = 1.0$$

$$L_b = 8 \text{ ft}$$

$$u_0 = Q/A =$$

$$\dot{m} = \beta Q$$

$$Q = \dot{m}/\beta$$

$$u_0 = \frac{\dot{m}/\beta}{A}$$

$$\text{Ergun Equation: } \Delta P = \frac{150 u_0 \mu L_b}{D_p^2} \cdot \frac{(1-\varepsilon)^2}{\varepsilon^3} + \frac{1.75 \beta u_0^2 L_b}{D_p} \cdot \frac{(1-\varepsilon)}{\varepsilon^3}$$

$$47.5 \frac{\text{lbm}}{\text{min}} \times \frac{1 \text{ min}}{60 \text{ s}} = 0.792 \text{ lbm/s}$$

$$\beta = \frac{(16.2 \frac{\text{lb}_f}{\text{ft}^2} \times \frac{144 \text{ in}^2}{\text{ft}^2}) (29 \frac{\text{lbm}}{\text{lbmol}})}{(1545.3 \frac{\text{ft}\cdot\text{lb}_f}{\text{R}\cdot\text{lbmol}}) (100^\circ\text{F})} = 0.438 \frac{\text{lbm}}{\text{ft}^3}$$

$$u_0 = \frac{0.792 \text{ lbm/s}}{\frac{0.438 \text{ lbm}}{\text{ft}^3} \cdot \frac{\pi (2 \text{ ft})^2}{4}} = 0.576 \text{ ft/s}$$

$$\Delta P = \frac{150 (0.576 \text{ ft/s}) (1.29 \times 10^{-5} \frac{\text{lbm}}{\text{ft}\cdot\text{s}}) (8 \text{ ft})}{(\frac{0.5}{12} \text{ ft})^2} \cdot \frac{(1-0.38)^2}{0.38^3} + \frac{1.75 (0.438 \frac{\text{lbm}}{\text{ft}^3}) (0.576 \text{ ft/s})^2 (8 \text{ ft})}{(\frac{0.5}{12} \text{ ft})^2} \cdot \frac{(1-0.38)}{0.38^3}$$

$$\Delta P = 553.2 \frac{\text{lb}_f}{\text{ft}^2} \times \frac{1 \text{ ft}^2}{144 \text{ in}^2}$$

$$\Delta P = 3.84 \text{ psi}$$