

4ii

$$\sin 2\theta - 1 = \cos 2\theta$$

(using identities $\sin 2\theta = 2 \sin \theta \cos \theta$
and $\cos 2\theta$ as $1 - 2\sin^2 \theta$)

$$2 \sin \theta \cos \theta - 1 = 1 - 2 \sin^2 \theta$$

$$2 \sin^2 \theta + 2 \sin \theta \cos \theta - 2 = 0$$

$$\sin^2 \theta + \sin \theta \cos \theta - 1 = 0$$

$$(As - 1 = \sin^2 \theta + \cos^2 \theta)$$

$$\sin^2 \theta + \sin \theta \cos \theta - (\sin^2 \theta + \cos^2 \theta) = 0$$

$$\sin \theta \cos \theta - \cos^2 \theta = 0$$

$$\cos \theta (\sin \theta - \cos \theta) = 0$$

Hence $\cos \theta = 0$ or $\sin \theta - \cos \theta = 0$

$$\cos \theta = 0$$

$$\text{at } 90^\circ \text{ or } 270^\circ$$

$$\frac{\pi}{2} \text{ and } \frac{3\pi}{2}$$

divide by $\cos \theta \neq 0$

$$\therefore \tan \theta - 1 = 0$$

$$\tan \theta = 1$$

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$$\theta = 45^\circ, \text{ or } 315^\circ$$

$$\text{Hence } \frac{\pi}{4} \text{ or } \frac{7\pi}{4}$$

$$\frac{\pi}{4}, \frac{\pi}{2}, \frac{3\pi}{2}, \frac{7\pi}{4} \quad (0 \leq \theta \leq 2\pi)$$