

Required	5kw	6.71	HJ	5000		
Pressure ratio		4:1				
Inlet Pressure Pa	2116200	21.162	bar		6894.757	306.9288736 psia
Inlet Temp C	70	158	F	617.67 R	343.15 K	

Cp	0.24 Btu/lbm	87 J/(kgK)	0.285714286	
γ	1.4		0.333333333	4
Rgas	53.34 ft-lbf/lbm-sec	287.04 J/kgK	0.730599956	

isentropic overall enthalpy drop

Δh isentropic	39.9360781 Btu/lbm		$\Delta h_{isentropic} = C_p \cdot T_o \cdot \left(1 - \left(\frac{1}{3}\right)^{\frac{\gamma-1}{\gamma}}\right)$	9763.764177 J/Kg
kasutegur	0.85			
tip clearance loss	5 %	0.95		

Actual enthalpy drop

ΔhOa	33.9456664 Btu/lbm		$\Delta h_{OA} = 0,85 \cdot \Delta h_{isentropic}$	8299.199551 J/Kg
------	--------------------	--	--	------------------

zero-clearance work

ΔhOazc	35.7322804 Btu/lbm		$\Delta h_{OAZC} = \frac{0,85}{0,95} \cdot \Delta h_{isentropic}$	8735.999527 J/Kg
--------	--------------------	--	---	------------------

required turbine flow

m	0.13973209 lbm/sec		$\dot{m} = \frac{P}{\Delta h_{OA}}$	0.7069 Btu/sec/hp	0.60246774 kg/s
---	--------------------	--	-------------------------------------	-------------------	-----------------

tip speed of the turbine

Co	1414.11486 ft/sec		$C_0 = \sqrt{2 \cdot \Delta h_{isentropic}}$	32.174 ft*lbm/lbf*sec ²	139.740933 m/s
				778.16 ft*lbf/Btu	

blade jet speed ratio

U1/Co	eq 42			
	0.7 optimum value			

wheel speed

U1	989.880399 ft/sec		$U_1 = 0,7 \cdot C_0$	97.8186531 m/s
----	-------------------	--	-----------------------	----------------

rotor inlet absolute tangential velocity component

V_{Θ1} 903.757614 ft/sec

required rotor blade count

Z_r 22.9876543

$$V_{\Theta 1} = \frac{\Delta h_{OAZC}}{U_1}$$

$$Z_r = \frac{2}{1 - \left(\frac{V_{\Theta 1}}{U_1}\right)}$$

89.30811507 m/s

22.98765432

we use 11 full and 11 splitter blades

22

recalculate absolute rotor inlet tangential velocity to the wheel speed

0.90909091

$$\frac{V_{\Theta 1}}{U_1} = 1 - \frac{2}{22}$$

0.909090909

required wheel speed

U₁ 992.004608 ft/sec

$$U_1 = \sqrt{\frac{\Delta h_{OAZC}}{V_{\Theta 1}/U_1}}$$

98.02856461 m/s

recalculate blade-jet ratio

0.70150215

$$\frac{U_1}{C_o}$$

0.701502148

absolute tangential velocity at rotor inlet

V_{Θ1} 901.822371 ft/sec

$$V_{\Theta 1} = \frac{V_{\Theta 1}}{U_1} \cdot U_1$$

89.11687692 m/s

Inlet critical velocity

α_{cr1} 1112.06631 ft/sec

$$\alpha_{cr1} = \sqrt{\frac{2 \cdot \gamma}{1 + \gamma} \cdot R_{gas} \cdot T_o}$$

V1

1036

338.9897816 m/s

v1

Rotor inlet density

ρ₁ 0.1278 lbm/ft³

$$\rho_1 = \frac{\rho_1'}{R_{gas} \cdot T_o} \cdot \left[1 - \frac{\gamma - 1}{\gamma + 1} \cdot \left(\frac{V_1}{\alpha_{cr1}} \right)^2 \right]^{\frac{1}{\gamma - 1}}$$

2381348.281 kg/m³

105

for the rotor exit vector diagram, we assume an exit flow coefficient φ₂ is 0,3

exit axial velocity

V_{x2} 297.601382 ft/sec

$$V_{x2} = \phi_2 \cdot U_1$$

29.40856938 m/s

to calculate rotor exit pressure, we need to know the critical Mach number at the exit

rotor exit total temperature

T₂ 468.785498 R

$$T_2 = T_o - \frac{\Delta h_{OAZC}}{C_p}$$

242.7362123 F

rotor exit critical velocity

α_{cr2} 1838.19154 ft/sec

$$\alpha_{cr2} = \sqrt{\frac{2 \cdot \gamma}{1 + \gamma} \cdot R_{gas} \cdot T_2}$$

285.1096329 m/s

static total pressure ratio at rotor exit is calculated from the gas dynamics reaction
 p_2/p_{prim2} 0.98479339

with the diffuser recovery assumed to be 0,4, rotor exit total pressure
 p_2 103.251689 psia

$$\frac{p_2}{p_2'} = \left[1 - \frac{\gamma-1}{\gamma+1} \cdot \left(\frac{V_2}{\alpha_{cr2}} \right)^2 \right]^{\frac{\gamma}{\gamma-1}} \quad 0.99380733$$

rotor exit density
 ρ_2 0.97505014 lbm/ft3

$$\rho_2 = \frac{\rho_2'}{R_{gas} \cdot T_0} \cdot \left[1 - \frac{\gamma-1}{\gamma+1} \cdot \left(\frac{V_2}{\alpha_{cr2}} \right)^2 \right]^{\frac{1}{\gamma-1}}$$

$$p_2' = \frac{P_{dis}}{R_p \cdot \left(1 - \frac{p_2}{p_2'} \right) + \frac{p_2}{p_2'}} \quad 531023.0704 \text{ Pa}$$

rotor exit volumetric flow
 Q_2 0.1433076 ft3/sec

$$Q_2 = \frac{\dot{m}}{\rho_2} \quad 0.112446162 \text{ m}^3/\text{s}$$

required rotor exit flow area
 A_2 2076.6616 in2

$$A_2 = \frac{\rho_2 \cdot V_{x2}}{\dot{m}} \quad 261.5346657 \text{ m}^2$$

correct head
 Δh^* isentropic 39.6520767 Btu/lbm

$$\Delta h^*_{isentropic} = C_p \cdot T_o \cdot \left(1 - \left(\frac{\rho_2}{44,1} \right)^{\frac{\gamma-1}{\gamma}} \right) \quad 29102.45487 \text{ J/kg}$$

rotational speed
 ω 49847.8656 rad/sec

$$\omega = \frac{N_s \cdot \Delta h^*_{isentropic}^{\frac{3}{4}}}{\sqrt{Q_2}} \quad \text{Ns} \quad 0.6 \quad 3986.815613 \text{ rad/s}$$

rotor inlet tip radius
 r_1 0.23880772 in

$$r_1 = \frac{U_1}{\omega} \quad 8.851747029 \text{ m}$$

rotor inlet blade height h_1
 h_1 0.39168206 in

$$h_1 = \frac{\dot{m}}{\rho_1 \cdot V_{r1} \cdot 2\Pi \cdot r_1} \quad \text{vr1} \quad 3.64093\text{E-}11 \text{ m}$$

rotor exit hub and tip radius
 r_{rms2} 0.13267096 in

$$r_{rms2} = \frac{r_1}{1,8} \quad \frac{r_1}{r_{rms2}} = 1,8 \quad \text{wing Rodg} \quad 4.917637238 \text{ m}$$

rh_2 #NUM! in

$$r_{h2} = \sqrt{r_{rms2}^2 - \frac{A_2^2}{\Pi}} \quad \text{#NUM!} \quad \text{m}$$

rt_2 828.678202 in

$$r_{t2} = \sqrt{r_{rms2}^2 + \frac{A_2^2}{\Pi}} \quad 147.6744531 \text{ m}$$