



at $t=0$,

m_{salt} in pool + lines = 10 kg

m_{salt} in collecting tank = 0 kg

at some time, all salt collects in tank.

Want to know $m_{\text{salt}}(t)$ in tank

$$\frac{dm_{\text{salt}}}{dt} = \text{in} - \text{out}$$

$$= \dot{m}_{\text{in}} \cdot \frac{m_{\text{salt}}(t)}{m_{\text{system}}} - \dot{m}_{\text{out}} \cdot \frac{m_{\text{salt}}(t)}{m_{\text{system}}}$$

$$\int \frac{dm_{\text{salt}}}{m_{\text{salt}}} = \int \frac{\dot{m}_{\text{in}}}{m_{\text{system}}} dt$$

$$\ln(m_{\text{salt}}) = \frac{\dot{m}_{\text{in}}}{m_{\text{system}}} t + C$$

$$m_{\text{salt}}(t) = A e^{\frac{\dot{m}_{\text{in}}}{m_{\text{system}}} t}$$

if $m_{\text{salt}}(0) = 0$,

$$0 = A e^0$$

$$A = 0$$

$$m_{\text{salt}}(t) = 0 \leftarrow \text{not right}$$

At some time, m_{salt} in tank will equal 10 kg. Not sure how to use this as boundary condition.

Look at it from pool's perspective.

$$\frac{dm_{\text{salt}}}{dt} = \overset{\text{concentration}}{\nearrow} \dot{m}_{\text{in}} - \dot{m}_{\text{out}} \quad \dot{m}_{\text{in}} = \dot{m}_{\text{out}}$$

$$\frac{dm_{\text{salt}}}{dt} = -\dot{m}_{\text{out}} \cdot \frac{m_{\text{salt}}}{m_{\text{system}}}$$

$$m_{\text{salt}}(t) = A e^{-\frac{\dot{m}_{\text{out}}}{m_{\text{system}}} \cdot t}$$

$$\text{if } m_{\text{salt}}(0) = 10 \text{ kg}$$

$$10 = A$$

$$m_{\text{salt}}(t) = \downarrow m_0 e^{-\frac{\dot{m}_{\text{out}}}{m_{\text{system}}} \cdot t}$$

Concentration in the tank must be opposite depletion in the pool.

$$\therefore m_{\text{salt}}(t)_{\text{(tank)}} = m_0 \left(1 - e^{-\frac{\dot{m}_{\text{out}}}{m_{\text{system}}} \cdot t} \right)$$