

S

$$C_{ij} = \sum_{k=1}^3 A_{ik} \cdot B_{kj}$$

Rotation tensor:

$$S' = R S R^T \Rightarrow S'_{ij} = \sum_{k=1}^K \sum_{l=1}^L R_{ik} \cdot R_{jl} \cdot S_{kl}$$

$$S = R^T S' R \Rightarrow S_{ij} = \sum_{l=1}^M \sum_{k=1}^N R_{mi} \cdot R_{nj} \cdot S'_{mn}$$

$$\Rightarrow A_{ik} = R_{mi} R_{nk} \cdot A'_{mn}$$

$$B_{kj} = R_{pk} R_{qj} B'_{pq}$$

the
proof $\Rightarrow C_{ij} = A_{ik} \cdot B_{kj} = (R_{mi} R_{nk} A'_{mn}) (R_{pk} R_{qj} B'_{pq})$

$$C_{ij} = R_{mi} R_{qj} A'_{mn} \cdot \underbrace{R_{nk} R_{pk} B'_{pq}}_{\text{need to be } B'_{kq}}$$

need to be
 B'_{kq}

$$\Rightarrow C_{ij} = R_{mi} R_{qj} \overbrace{A'_{mn} B'_{kq}}^{C'_{mq}}$$

$$\Rightarrow C_{ij} = R_{mi} R_{qj} C'_{mq}$$

prove