

Use multiplication or division of power series to find the first three nonzero terms in the Maclaurin series for the given function.

$$e^x \ln\left(1 - \frac{x}{5}\right) \approx v + z + y + \dots$$

$$\ln\left(1 - \frac{x}{5}\right) = \int \frac{-dx}{5(1 - \frac{x}{5})} = -\frac{1}{5} \sum_{n=0}^{\infty} \left(\frac{x}{5}\right)^n = -\sum_{n=0}^{\infty} \left(\frac{x}{5}\right)^{n+1} \frac{1}{(n+1)}$$

or:

$$\sum_{n=0}^{\infty} \frac{f^{(n)}(0)}{n!} x^n = \sum_{n=0}^{\infty} \frac{(-1)(n-1)!}{5^n n!} (x)^n = \ln(1) + \sum_{n=1}^{\infty} \frac{(-1)}{5^n * n} x^n = \sum_{n=0}^{\infty} \frac{(-1)x^{n+1}}{5^{n+1}(n+1)}$$

$$f^{(0)}(x) = \ln\left(1 - \frac{x}{5}\right) \rightarrow f^{(0)}(0) = \ln(1) = 0$$

$$f^{(1)}(x) = \frac{-1}{5-x} \rightarrow f^{(1)}(0) = \frac{-1}{5}$$

$$f^{(2)}(x) = \frac{-1}{(5-x)^2} \rightarrow f^{(2)}(0) = \frac{-1}{5^2} = -\frac{1}{25}$$

$$f^{(3)}(x) = \frac{-2}{(5-x)^3} \rightarrow f^{(3)}(0) = \frac{-2}{5^3} = \frac{-2}{125}$$

$$f^{(4)}(x) = \frac{-2 * 3}{(5-x)^4} \rightarrow f^{(4)}(0) = \frac{-2 * 3}{5^4}$$

$$f^{(n)}(x) = \frac{(-1) * (n-1)!}{(5-x)^n} \rightarrow f^{(n)}(0) = \frac{(-1)(n-1)!}{5^n}$$

$$\left(\sum_{n=0}^{\infty} \frac{x^n}{n!}\right) \left(-\sum_{n=0}^{\infty} \left(\frac{x}{5}\right)^{n+1} \frac{1}{(n+1)}\right) =$$

$$\left(1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots\right) \left(-\frac{x}{5 * 1} - \frac{x^2}{5^2 * 2} - \frac{x^3}{5^3 * 3} - \frac{x^4}{5^4 * 4} - \dots\right)$$

$$\left(1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots\right) \left(-\frac{x}{5} - \frac{x^2}{50} - \frac{x^3}{375} - \frac{x^4}{2500} - \dots\right)$$

$$1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$$

$$* -\frac{x}{5} - \frac{x^2}{50} - \frac{x^3}{375} + \dots$$

$$-\frac{x}{5} - \frac{x^2}{5} - \frac{x^3}{10} - \frac{x^4}{30}$$

$$+ -\frac{x^2}{50} - \frac{x^3}{50} - \frac{x^4}{50 * 2!} - \frac{x^5}{50 * 3!}$$

$$-\frac{x}{5} - \frac{11x^2}{50} - \frac{3x^3}{25} + \dots$$