

Example 1.3: The diameter and length of a metal cylinder measured with the help of vernier callipers of least count 0.01 cm are 1.22 cm and 5.35 cm. Calculate the volume V of the cylinder and uncertainty in it.

Solution: Given data is

Diameter $d = 1.22$ cm with least count 0.01 cm

Length $l = 5.35$ cm with least count 0.01 cm

Absolute uncertainty in length = 0.01 cm

$$\% \text{age uncertainty in length} = \frac{0.01 \text{ cm}}{5.35 \text{ cm}} \times 100 = 0.2\%$$

Absolute uncertainty in diameter = 0.01 cm

$$\% \text{age uncertainty in diameter} = \frac{0.01 \text{ cm}}{1.22 \text{ cm}} \times 100 = 0.8\%$$

As volume is $V = \frac{\pi d^2 l}{4}$

$$\begin{aligned} \therefore \text{total uncertainty in } V &= 2 (\% \text{age uncertainty in diameter}) \\ &+ (\% \text{age uncertainty in length}) \\ &= 2 \times 0.8 + 0.2 = 1.8\% \end{aligned}$$

$$\text{Then } V = \frac{3.14 \times (1.22 \text{ cm})^2 \times 5.35 \text{ cm}}{4} = 6.2509079 \text{ cm}^3 \text{ with } 1.8\% \text{ uncertainty}$$

Thus $V = (6.2 \pm 0.1) \text{ cm}^3$

Where 6.2 cm^3 is calculated volume and 0.1 cm^3 is the uncertainty in it.

This is an example from my textbook.

My objection is that there should be three significant figures in the final answer 6.25 cm^3 , as least number of significant figures in measurement (diameter and length both) is three. Moreover, the absolute uncertainty should be 0.11 cm^3 with two decimal places as present in 6.25 cm^3 .