

sign convention

Tension (+)
Compression (-)

Ductile: mat'l with more than 5% elongation at fracture (P.62)

STRESS analysis

Tension-compression $\sigma_{max} = P/A$

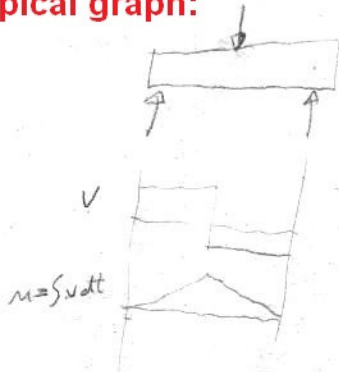
Basics $T_{max} = T/\bar{A}$

Bending $\sigma_{max} = \frac{Mc}{I}$

Bending Rectangular: $T_{max} = \frac{3V}{2A}$

Circular: $T_{max} = \frac{4V}{3A}$

typical graph:



Mohr's circle

$$\sigma_1, \sigma_3 = \frac{\sigma_x + \sigma_y}{2} \pm \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2}$$

$$T_{max} = \frac{|\sigma_1 - \sigma_3|}{2}$$

$\sigma_1 > \sigma_3$ $\tau_{xy} + \text{CW}$
 $\tau_{xy} - \text{CCW}$

$$\tan 2\phi = \frac{2\tau_{xy}}{\sigma_x - \sigma_y}$$

sign convention
/

criteria
(safest to
unsafest)

(SAFE)

MAX shear

$$N = \frac{S_y}{2T_{max}}$$

Von Mises

$$N = \frac{S_y}{\sigma'}$$

Max strain

$$N = \frac{S_y}{\sigma'}$$

(UNSAFE)

Max Normal

$$N = \frac{S_y}{|\sigma_{max}|}$$

$$\sigma' = \sqrt{\sigma_1^2 + \sigma_2^2 - \sigma_1\sigma_2}$$

$$\sigma' = |\sigma_{max} - \sigma_{min}|$$

$$\sigma_{max} = \max(|\sigma_1|, |\sigma_3|)$$

$$\sigma_{min} = \min(|\sigma_1|, |\sigma_3|)$$

with their respective signs

For brittle mat'l:

Coulomb-Mohr

$$\sigma_3 < 0 \rightarrow \frac{1}{N} = \frac{\sigma_1}{S_{ut}} - \frac{\sigma_3}{S_{uc}}$$

$$\sigma_3 > 0 \rightarrow N = \frac{S_{ut}}{\sigma_1}$$

Modified Mohr

$$\frac{-\sigma_3}{\sigma_1} > 1 \rightarrow \frac{1}{N} = \frac{\sigma_1}{S_{ut}} - \frac{\sigma_3}{S_{uc}} - \frac{\sigma_1}{S_{uc}}$$

$$\frac{-\sigma_3}{\sigma_1} < 1 \rightarrow N = \frac{S_{ut}}{\sigma_1}$$

For impact:

IMPACT

$$I.F. = \frac{F_i}{W} = 1 + \sqrt{1 + \frac{2h\eta}{\delta_{st}}}$$

$$= v_i \sqrt{\frac{\eta}{g\delta_{st}}}$$

$$M = F(F_i) \Rightarrow \sigma = \frac{Mc}{I}$$

$$\eta = \frac{1}{1 + \frac{m_b}{3m}}$$

$m_b \rightarrow$ struck object
 $m \rightarrow$ striking object

For notches:

NOTCHES

$$\sigma = K_t \sigma_{nom}$$

$$\sigma = K_f \sigma_{nom}$$

$$T = K_{ts} T_{nom}$$

$$T = K_{fs} T_{nom}$$

$K_t \rightarrow$ geometric factor (static) \rightarrow Tables

\rightarrow for ductile ($K_t = 1$) \rightarrow although use small d at notch for $\sigma = \frac{Mc}{I}$

$K_f \rightarrow$ geometric factor (dynamic)

$$K_f = 1 + q(K_t - 1)$$

\rightarrow often alternating stress see P.390

$$q = \left(1 + \frac{\sqrt{a}}{\sqrt{r}}\right)^{-1}$$

\rightarrow notch radius

\rightarrow Table (P.390) (P.391)

SHAFT

Fatigue strength (S_f), Endurance limit (S_e) \rightarrow P.33-36 (notes)

For shaft:

Agg \rightarrow Fig. 6-25 (P.377)

C reliability \rightarrow Table (P.381)

$$N = \frac{S_e}{K_f \sigma_{nom}} \text{ (dynamic)} \quad N = \frac{S_y}{K_t \sigma_{nom}} \text{ (static)}$$

$$K_f \sigma_{nom}$$

$\rightarrow \sigma_a$ (when $\sigma_m = 0$)
(see other side)

$$K_t \sigma_{nom} \text{ (} K_t = 1 \text{ ductile)}$$

\rightarrow critical sections \rightarrow all steps + mid length of shaft

\rightarrow use small ϕ to find $\sigma_{nom} = \frac{Mc}{I}$

For fatigue:

cumulative fatigue damage \rightarrow P.66

Fatigue

$$\sigma_a = \frac{\sigma_{max} - \sigma_{min}}{2}$$

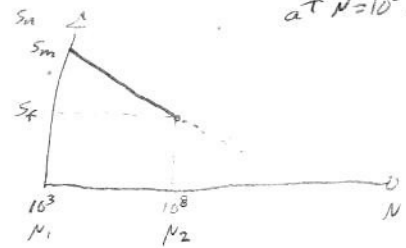
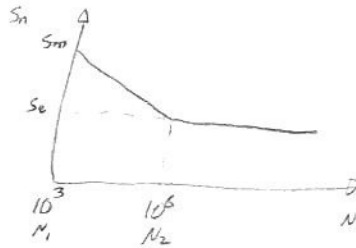
$$\sigma_m = \frac{\sigma_{max} + \sigma_{min}}{2}$$

SAFETY Factor for fluctuating stress \rightarrow P.43 (notes)

Equation for graph \rightarrow

bending $S_m = 0.9 S_{ut}$

axial loading $S_m = 0.75 S_{ut}$



at $N=10^8 \rightarrow S_n = S_{ut}$

$$\log S_n = \log a + b \log N$$

$$S_n = a N^b$$

$$z = \log N_1 - \log N_2$$

$$b = \frac{1}{z} \log \left[\frac{S_m}{S_e} \right] \quad \log a = \log S_m - 3b$$

Fully reversed (-F to F) $\sigma_m = 0$

Steps \rightarrow Find: $K_T, S_{ut}, S_y, S_e', q, K_f, \sigma_{a, nom}, \sigma_a, \sigma, \sigma_3, \sigma', S_e, S_n, \Rightarrow N_f = \frac{S_n}{\sigma'}$

Repeated or Fluctuating ($\sigma_m \neq 0$)

P.42 $\sigma_{m, nom}$ (P.42 notes)

Steps \rightarrow Find: $K_T, q, K_f, \sigma_{a, nom}, \sigma_a, \sigma_{m, nom}, \sigma_m, S_{ut}, S_y, S_e'$ ($T_{a, nom}, T_{a, min}, T_{m, nom}, T_{m, min}$ etc)

$\sigma_a', \sigma_m', S_e, S_n \Rightarrow N_f \rightarrow$ see P.4 notes where $S_f = S_n$

$$\sigma_a' = \sqrt{\sigma_{xa}^2 + \sigma_{ya}^2 - \sigma_{xya} + 3T_{xya}^2}$$

$$\sigma_m' = \sqrt{\sigma_{xm}^2 + \sigma_{ym}^2 - \sigma_{xym} + 3T_{xym}^2}$$

Screws + Fasteners \rightarrow P.53

stress in threads \rightarrow P.57

Self-locking screw if: $\mu \geq \frac{L}{\pi d_p} \cos \alpha$ ($\mu \geq \tan \lambda \cos \alpha$)
(opposite is back-driving: $\mu < \tan \lambda \cos \alpha$)

Fastener in shear \rightarrow P.63

Gears $d = \frac{N}{P_d/t}$ $P_c = \frac{\pi d}{N}$ $P_c P_{dt} = \pi$ ($P_{dt} = (P_{dt}) \cos \psi$)

$$n_1 P_1 a + n_2 P_2 b = M$$

load on gears: $F_t = \frac{2T}{d}$ $F_r = F_t \tan \phi$ $F = \frac{F_t}{\cos \phi}$

$$\frac{P_1}{a} = \frac{P_2}{b} \quad c = \frac{d_p + d_g}{2} = \frac{N_p + N_g}{2(P_d)_c}$$

standard \rightarrow P.715
contact ratio $m_p = \frac{z}{P_b} = \frac{N z}{\pi d \cos \phi} = \frac{P_d z}{\pi \cos \phi}$ \rightarrow P.708

bending \rightarrow P.74

$$N = \frac{S_{fb}}{\sigma_b}$$

\cdot Lo P.70

surface contact \rightarrow P.75

$$N = \frac{S_{fc}}{\sigma_c}$$

Lo P.71