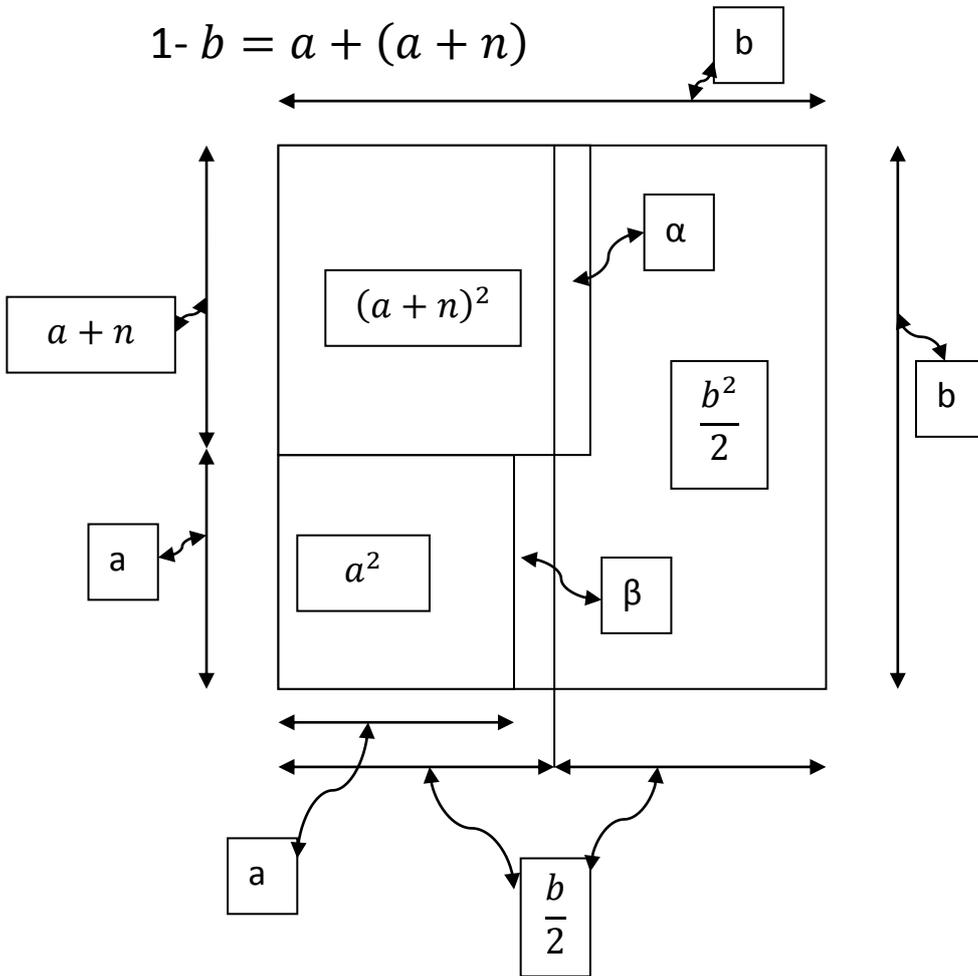


$$1- b = a + (a + n)$$



$$2- b^2 = a^2 + (a + n)^2 + \beta - \alpha + \frac{b^2}{2}$$

$$3- \beta = a \left( \frac{b}{2} - a \right)$$

$$4- \alpha = (a + n) \left( a + n - \frac{b}{2} \right)$$

$$5- b^2 = a^2 + (a + n)^2 + \frac{b^2}{2} - \left( (a + n) \left( a + n - \frac{b}{2} \right) - a \left( \frac{b}{2} - a \right) \right)$$

6- We multiply each side by:  $b^{k-2}$

$$7- b^k = a^2 b^{k-2} + (a + n)^2 b^{k-2} + \frac{b^k}{2} - b^{k-2} \left( (a + n) \left( a + n - \frac{b}{2} \right) - a \left( \frac{b}{2} - a \right) \right)$$

8- From 7 we deduce:  $b^k = x^k + y^k$

$$9- x^k = \frac{b^k}{2}$$

$$10- y^k = a^2 b^{k-2} + (a + n)^2 b^{k-2} - b^{k-2} \left( (a + n) \left( a + n - \frac{b}{2} \right) - a \left( \frac{b}{2} - a \right) \right)$$

11-  $b$  is odd  $\xrightarrow{\text{yields}}$   $b^k$  is odd  $\xrightarrow{\text{yields}}$   $\frac{b^k}{2}$  is not an integer

12- From 11 we deduce that  $x^k$  is not an integer and so is  $x$

13- If  $b = a + (a + n)$  and  $b$  is odd then  $b^k = x^k + y^k$  does not have integer solutions.

14- If  $b$  is even then  $n = 0$

$$15- \text{From 14: } b^k = 2a^2 b^{k-2} + \frac{b^k}{2} \text{ and } a = \frac{b}{2}$$

16- From 15:  $b^k$  can only be the sum of its halves.

