

Problem Statement

A system of equations and BC's governs the manner fluid oscillates in a 2D rectangular channel. Applying the Ritz method to these, we arrive at an algebraic eigenvalue problem:

$$\mathbf{M} + \lambda i \mathbf{\Phi} + \lambda^2 \mathbf{K} = \mathbf{0} \quad (1)$$

where $\mathbf{M}, \mathbf{\Phi}, \mathbf{K}$ are real constant $N \times N$ matrices. This problem admits analytic eigenvalues λ , the first few listed:

$$\lambda_{1,2,3} = \pm -2.4803 + 0.0173i, \pm 10.5719 + 0.1160i, \pm 22.2756 + 0.313425i \quad (2)$$

Another way to solve for the eigenvalues of (1) is to introduce a forcing term, which augments the system

$$\mathbf{M} + \omega i \mathbf{\Phi} + \omega^2 \mathbf{K} = \omega \mathbf{F}, \quad (3)$$

where \mathbf{F} is a real constant $1 \times N$ vector. Note λ has been “changed” to the forcing frequency ω , a user selected parameter. Then (3) is not an eigenvalue problem, but rather a linear system of equations taking the form $\mathbf{A}x = \mathbf{b}$. Specifying a value ω yields a complex vector solution to (3), denoted \mathbf{C} . Performing a frequency scan, we input several values of ω and plot the magnitude $|\mathbf{C}|$, shown in figure 1.

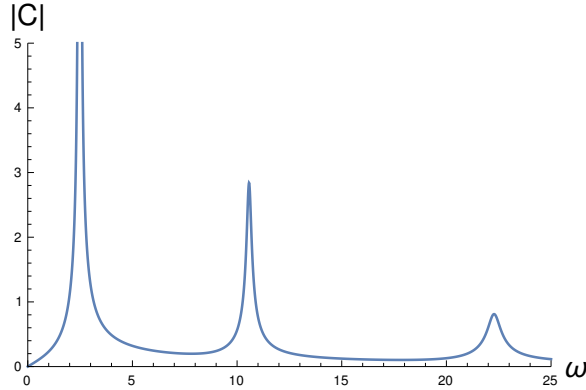


Figure 1: Response diagram corresponding to (3).

Denote ω_k the value corresponding to the k^{th} peaks of figure 1. We observe $|\lambda_1| = 2.4804 = \omega_1$, which in fact holds for all k . My question is: how can we separate ω_k into its real and imaginary components? I was told this is a fairly regular problem for people studying controls.