

**Given:**

$$q_1 = 5 \text{ m}^3/\text{s}$$

$$h_1 = 75 \text{ ft} = 22.860 \text{ m}$$

$$h_2 = 70 \text{ ft} = 21.336 \text{ m}$$

$$\rho = 1000 \text{ kg/m}^3 \text{ is density of water}$$

$$g = 9.81 \text{ m/s}^2 \text{ is acceleration due to gravity}$$

**Solution:**

(1) In absence of water in the tank A the power output of the turbine is equal to decrease in gravitational potential energy of the water which is given by

$$W_1 = \rho * g * h_1 * q_1 = 1000 * 9.81 * 22.86 * 5 = 1.121 * 10^6 \text{ W} = 1.121 \text{ MW}$$

The speed of water flow is given by

$$v_1 = \sqrt{2 * g * h_1} = \text{sqr}(2 * 9.81 * 22.860) = 21.18 \text{ m/s}$$

Let A be cross sectional are of the tube. Then the volume water flow is given by

$$q_1 = A * v_1$$

From which we get

$$A = q_1 / v_1 = 5 / 21.18 = 0.2361 \text{ m}^2$$

Now consider when the draft tube is at 70 feet below the water surface

Now the speed of water flow is given by

$$v_2 = \sqrt{2 * g * (h_1 - h_2)} = \text{sqr}[2 * 9.81 * (22.860 - 21.336)] = 5.468 \text{ m/s}$$

So the new volume water flow is given by

$$q_2 = A \cdot v_2 = 0.2361 \cdot 5.468 = 1.291 \text{ m}^3/\text{s}$$

Comparing it with  $q_1$  we conclude that the volume water flow through the turbine reduces

(2) The water is incompressible, so the water flow rate is the same in the draft tube. Therefore the output at the end of the draft tube is the same as at its input

$$q_{\text{out}} = q_2 = 1.291 \text{ m}^3/\text{s}$$

(3) The new output power of the turbine at the end of the draft tube is given by

$$W_2 = \rho \cdot g \cdot (h_1 - h_2) \cdot q_2 = 1000 \cdot 9.81 \cdot (22.860 - 21.336) \cdot 1.291 = 1.930 \cdot 10^4 \text{ W} = 19.30 \text{ kW}$$

Comparing it with  $W_1$  we conclude that the power of the turbine reduces