

As demonstrated in Fig. 1, the red circuit (fig. 1-(a)) is rotated around Z axis, thus forming a space, Γ (Fig. 1-b). In this space, the function $C(x,y,z)$ meets the Laplace equation,

$$\frac{\partial^2 C}{\partial x^2} + \frac{\partial^2 C}{\partial y^2} + \frac{\partial^2 C}{\partial z^2} = 0$$

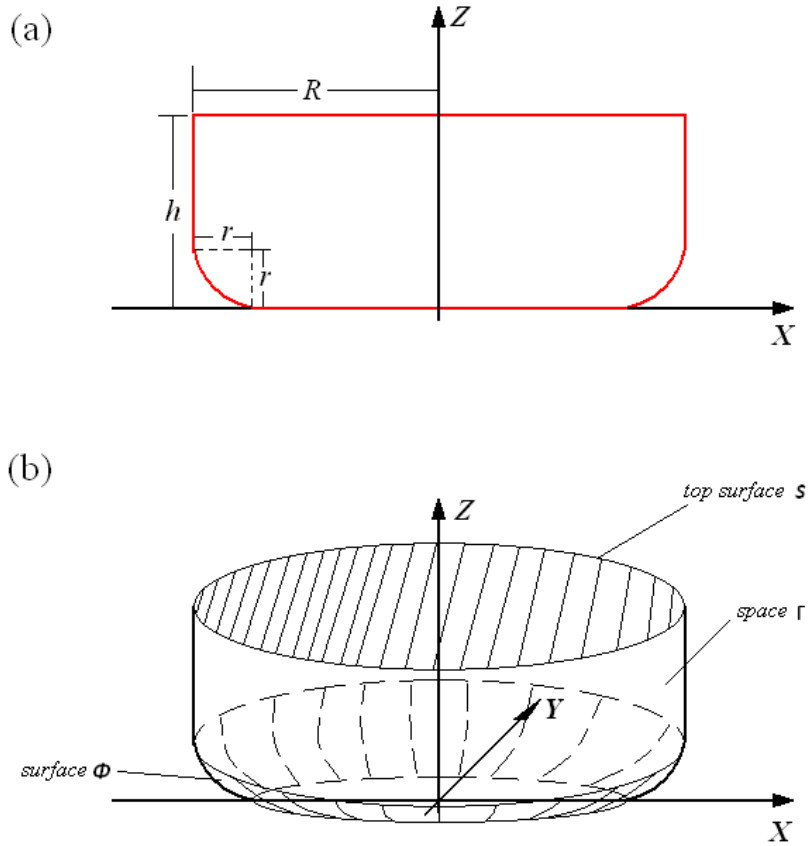


图 1

The boundary condition is listed below,

- (1) At the top surface, S , $C=a\theta$, $0 < a < 1$, (S is described by $z=h, x^2 + y^2 \leq R^2$) ;
- (2) At the surface, Φ , $C = \theta$ (Φ is defined by rotation of the quarter circle shown in Fig. 1-a, which is described by, $z = r - \sqrt{r^2 - [\sqrt{x^2 + y^2} - (R-r)]^2}$) ;
- (3) In the space, Γ , $C(x,y,z)$ is a constant at the circles described by

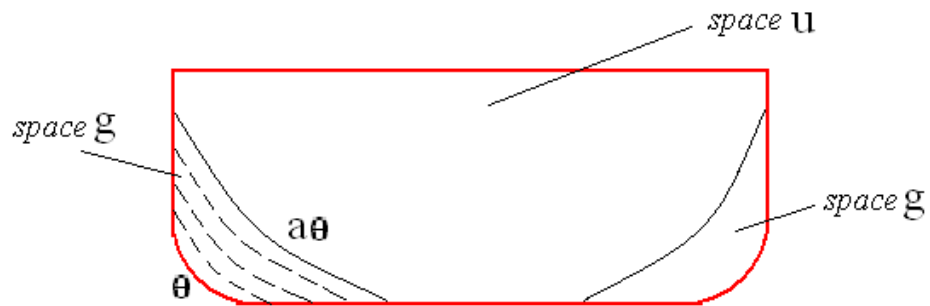
$$x^2 + y^2 = a^2, z = b (0 \leq a \leq R, 0 \leq z \leq h), \text{ which means } \frac{\partial C}{\partial x} = 0, \frac{\partial C}{\partial y} = 0 \text{ at these}$$

; circles

Question 1: $C(x, y, z) = ?$

(2) if $\rho(x, y, z) = \frac{\partial C}{\partial x} + \frac{\partial C}{\partial y} + \frac{\partial C}{\partial z}$, then, $\iint_{\phi} \rho(x, y, z) ds = ?$

P.S.: (1) this is math model of a practical diffusion process. Practically, the solution may be demonstrated in the following figure,



in space \mathbf{U} , $C(x, y, z) = a\theta$,
 in space \mathbf{G} , there is a
 gradient from θ to $a\theta$

(2) if the precise solution cannot be deduced, the approximation solution also is OK.