

## Homework 3 – Due September 30

3.1. (20 pt.) Two infinitely long filaments are placed parallel to the  $x$ -axis as shown in Figure 1.

a) Find  $H$  at the origin;

a) Find  $H$  at  $(-1,2,2)$ ;

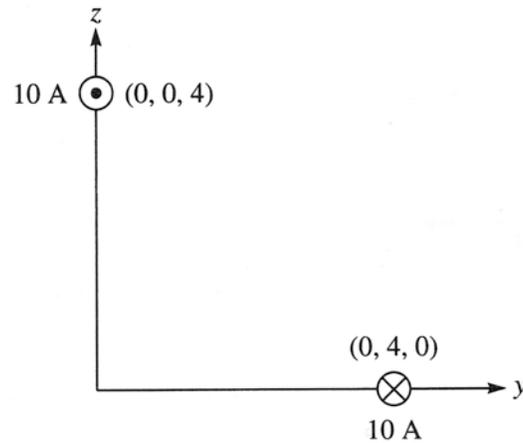


Figure 1

3.2. (20 pt.) A long, straight wire of radius  $a$  has current density  $J = J_0 e^{-\beta(\alpha-\rho)} u_z$  where  $\beta$  is a constant and  $\rho < a$ . Determine  $B$  inside and outside the wire.

3.3. (25 pt.) A conductor that is 2 m long and is carrying a current of 3 A is placed parallel to the  $z$ -axis at a distance  $\rho_0 = 10$  cm as shown in Figure 2.

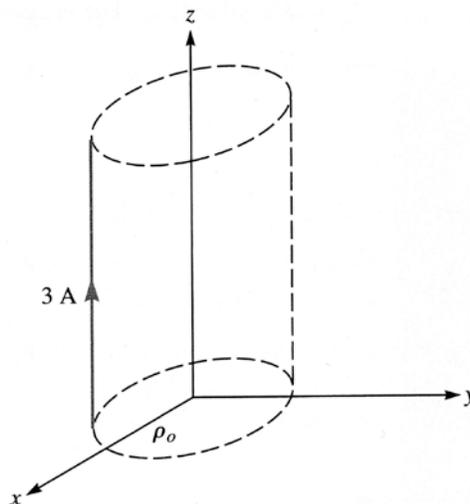


Figure 2

If the magnetic field in the region is  $\cos\frac{\varphi}{3}u_\rho \frac{Wb}{m^2}$ , how much work is required to rotate the conductor one revolution about the  $z$ -axis?

3.4. (25 pt.) Consider the magnetic circuit shown in Figure 3.

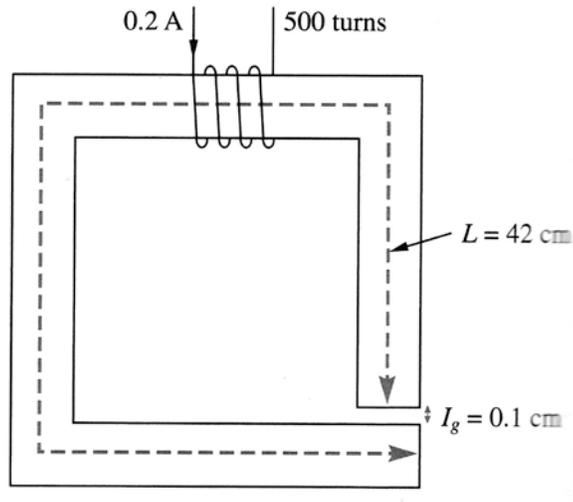


Figure 3

Assuming that the core ( $\mu_r = 1000$ ) has a uniform cross section of  $4 \text{ cm}^2$ , determine the flux density in the air gap.

3.5. (10 pt.) The current density in a cylindrical conductor of radius  $a$  placed along the  $z$ -axis is

$$J = 10e^{-\left(1-\frac{\rho}{a}\right)}u_z \frac{A}{m^2}$$

Find the current through the cross-section of the conductor.