

This time we consider $\Delta y \neq 0, \Delta z \neq 0$

$$\begin{aligned}
\begin{bmatrix} 0 \\ \Delta x' \\ \Delta y' \\ \Delta z' \end{bmatrix} &= \begin{bmatrix} \gamma & -\beta_x \gamma & -\beta_y \gamma & -\beta_z \gamma \\ -\beta_x \gamma & 1+(\gamma-1)\frac{\beta_x^2}{\beta^2} & (\gamma-1)\frac{\beta_x \beta_y}{\beta^2} & (\gamma-1)\frac{\beta_x \beta_z}{\beta^2} \\ -\beta_y \gamma & (\gamma-1)\frac{\beta_x \beta_y}{\beta^2} & 1+(\gamma-1)\frac{\beta_y^2}{\beta^2} & (\gamma-1)\frac{\beta_y \beta_z}{\beta^2} \\ -\beta_z \gamma & (\gamma-1)\frac{\beta_x \beta_z}{\beta^2} & (\gamma-1)\frac{\beta_y \beta_z}{\beta^2} & 1+(\gamma-1)\frac{\beta_z^2}{\beta^2} \end{bmatrix} \begin{bmatrix} c\Delta t \\ \Delta x \\ \Delta y \\ \Delta z \end{bmatrix} = \\
&= \begin{bmatrix} \gamma & -\beta_x \gamma & -\beta_y \gamma & -\beta_z \gamma \\ -\beta_x \gamma & 1+(\gamma-1)\frac{\beta_x^2}{\beta^2} & (\gamma-1)\frac{\beta_x \beta_y}{\beta^2} & (\gamma-1)\frac{\beta_x \beta_z}{\beta^2} \\ -\beta_y \gamma & (\gamma-1)\frac{\beta_x \beta_y}{\beta^2} & 1+(\gamma-1)\frac{\beta_y^2}{\beta^2} & (\gamma-1)\frac{\beta_y \beta_z}{\beta^2} \\ -\beta_z \gamma & (\gamma-1)\frac{\beta_x \beta_z}{\beta^2} & (\gamma-1)\frac{\beta_y \beta_z}{\beta^2} & 1+(\gamma-1)\frac{\beta_z^2}{\beta^2} \end{bmatrix} \left(\begin{bmatrix} c\Delta t \\ \Delta x \\ 0 \\ 0 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ \Delta y \\ 0 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 0 \\ \Delta z \end{bmatrix} \right) = \\
&= \begin{bmatrix} \gamma & -\beta_x \gamma & -\beta_y \gamma & -\beta_z \gamma \\ -\beta_x \gamma & 1+(\gamma-1)\frac{\beta_x^2}{\beta^2} & (\gamma-1)\frac{\beta_x \beta_y}{\beta^2} & (\gamma-1)\frac{\beta_x \beta_z}{\beta^2} \\ -\beta_y \gamma & (\gamma-1)\frac{\beta_x \beta_y}{\beta^2} & 1+(\gamma-1)\frac{\beta_y^2}{\beta^2} & (\gamma-1)\frac{\beta_y \beta_z}{\beta^2} \\ -\beta_z \gamma & (\gamma-1)\frac{\beta_x \beta_z}{\beta^2} & (\gamma-1)\frac{\beta_y \beta_z}{\beta^2} & 1+(\gamma-1)\frac{\beta_z^2}{\beta^2} \end{bmatrix} \left(\begin{bmatrix} \beta_x \Delta x \\ \Delta x \\ 0 \\ 0 \end{bmatrix} + \begin{bmatrix} \beta_y \Delta y \\ 0 \\ \Delta y \\ 0 \end{bmatrix} + \begin{bmatrix} \beta_z \Delta z \\ 0 \\ 0 \\ \Delta z \end{bmatrix} \right)
\end{aligned}$$

where $\beta_x = \frac{v_x}{c}, \beta_y = \frac{v_y}{c}, \beta_z = \frac{v_z}{c}$