

$$\frac{d^2}{dx^2}(y) - 4(x) = f(x,y)$$

here we have double derivative of y wrt x  
y is dependent variable and x is independent  
variable  
and both y and its derivative are in first degree  
and well they are not multiplied together so  
acc to my book this is LDE

but now i will try to prove its linearity by  
superposition principle the one which we have  
been taught in earlier classes to solve whether  
the equations are linear or not but now i am  
going to apply it to differential equations to  
check its linearity

$$f(x_1, y_1) = \frac{d^2}{dx^2}(y_1) - 4(x_1)^2$$

$$f(x_2, y_2) = \frac{d^2}{dx^2}(y_2) - 4(x_2)^2$$

that y is our dependent variable  
because we always left with additional  
factor of  $8 \cdot x_1 \cdot x_2$  by putting  $x = x_1 + x_2$   
since the linearity of function is impossible to  
prove by considering superposition  
principle unless we think of new way to  
prove it : MULTILINEARITY