



L = length of the rope, $L \in \mathbb{R}$ constant
 m = mass of the object.

From Diagram 2: ~~$x(t)$~~

$$\sin[\theta(t)] = \frac{x(t)}{L} \Rightarrow \boxed{x(t) = L \cdot \sin[\theta(t)]}$$

$$\cos[\theta(t)] = \frac{y(t)}{L} \Rightarrow \boxed{y(t) = L \cdot \cos[\theta(t)]}$$

$$\vec{r}(t) = x(t) \hat{x}_0 + y(t) \hat{y}_0 \Rightarrow \boxed{\vec{r}(t) = L \cdot \sin[\theta(t)] \hat{x}_0 + L \cos[\theta(t)] \hat{y}_0}$$

$$\text{or } \boxed{\vec{r}(t) = L \cdot \{ \sin[\theta(t)] \hat{x}_0 + \cos[\theta(t)] \hat{y}_0 \}} \quad \text{a}$$

$$|\vec{r}(t)| = \sqrt{L^2 \sin^2[\theta(t)] + L^2 \cos^2[\theta(t)]} = \sqrt{L^2 \{ \sin^2[\theta(t)] + \cos^2[\theta(t)] \}}$$

$$= \sqrt{L^2 \cdot 1} \Rightarrow \boxed{|\vec{r}(t)| = L} \quad \text{b}$$

$$\frac{\partial \vec{r}(t)}{\partial t} = L \cdot \left\{ \cos[\theta(t)] \cdot \frac{\partial \theta(t)}{\partial t} \hat{x}_0 - \sin[\theta(t)] \cdot \frac{\partial \theta(t)}{\partial t} \hat{y}_0 \right\}$$

$$\Rightarrow \vec{v}(t) = L \cdot \{ \omega(t) \cdot \cos[\theta(t)] \hat{x}_0 - \omega(t) \cdot \sin[\theta(t)] \hat{y}_0 \}$$

$$\boxed{\vec{v}(t) = L \cdot \omega(t) \cdot \{ \cos[\theta(t)] \hat{x}_0 - \sin[\theta(t)] \hat{y}_0 \}} \quad \text{c}$$

$$|\vec{v}(t)| = \sqrt{L^2 \omega(t)^2 \cos^2[\theta(t)] + L^2 \omega(t)^2 \sin^2[\theta(t)]} \Rightarrow \boxed{|\vec{v}(t)| = L \cdot \omega(t)} \quad \text{d}$$

$$a_T = \frac{\partial |\vec{v}(t)|}{\partial t} = \frac{\partial}{\partial t} [L \cdot \omega(t)] = L \cdot \frac{\partial \omega(t)}{\partial t}$$

$$\Rightarrow \boxed{a_T = L \cdot \frac{\partial \omega(t)}{\partial t}} \text{ (e)}$$

$$a_N = \frac{|\vec{v}|^2}{R} = \frac{[L \cdot \omega(t)]^2}{L} = \frac{L \cdot \omega(t)^2}{1}$$

$$\Rightarrow \boxed{a_N = L \cdot \omega(t)^2} \text{ (f)}$$

Newton's Law 2 - Diagram (g)

$$\sum \vec{F} = m \cdot \vec{a} \Rightarrow \vec{W} + \vec{T} = m \cdot \vec{a} \Rightarrow \text{mg} + \vec{T}$$

$$\Rightarrow -m \cdot g \hat{y}_0 + \vec{T} = m \cdot \vec{a}$$

$$\Rightarrow -mg \hat{y}_0 + T_1 \hat{x}_0 + T_2 \hat{y}_0 = m \cdot (a_1 \hat{x}_0 + a_2 \hat{y}_0)$$

$$\Rightarrow -g \hat{y}_0 + \frac{T_1}{m} \hat{x}_0 + \frac{T_2}{m} \hat{y}_0 = a_1 \hat{x}_0 + a_2 \hat{y}_0$$

$$\boxed{a_1 = \frac{T_1}{m}} \text{ (g)}$$

$$\boxed{a_2 = -g + \frac{T_2}{m}} \text{ (h)}$$

if only $a_1 \equiv a_N$ and $a_2 \equiv a_T$
then I can find T_1 and T_2 , but
I'm not sure if this is true.

a_1, a_2 are in the X-Y dimension
but a_T, a_N in 3D space.