



Darcy - Weisbach Equation for Pressure Loss over a Length of Pipe :

$$\Delta P_{friction} = f \frac{L}{D} \frac{\rho v^2}{2}$$

$\Delta P_{friction}$  - Pressure Drop over Pipe [Pa]

$f = \lambda$  - Friction Factor

$L$  - Length of Pipe [m]

$D$  - Hydraulic Diameter of Pipe [m]  $D = 2r$  for a circular c/s

$\rho$  - Density of Fluid [kg/m<sup>3</sup>]

$v$  - Average Velocity of Fluid Flow [m/s]

Bernoulli's Equation :

$$P + \frac{1}{2} \rho v^2 + \rho gh = \text{Constant}$$

$P$  - Pressure [Pa]

$\rho$  - Density of Fluid [kg/m<sup>3</sup>]

$v$  - Average Velocity of Fluid Flow [m/s]

$g$  - Gravitational Acceleration  $g = 9,81$  [m/s<sup>2</sup>]

$h$  - Height above or below Mean [m]

The valve is opened rapidly.

So putting the two equations together for this problem:

$$P_1 + \frac{1}{2}\rho v_1^2 + \rho g h_1 = P_2 + \frac{1}{2}\rho v_2^2 + \rho g h_2 + \Delta P_{friction}$$

Assuming densities are the same and that  $h_2$  is on the reference line,  $h_1 = -h$ , and that  $v_1$  is negligible compared to  $v_2$  (large container, small pipe area) and rearranging:

$$P_1 - P_2 - \rho g h = \frac{1}{2}\rho v_2^2 + f \frac{L}{D} \frac{\rho v_2^2}{2}$$

$D = d$  in this example.

Making  $v_2$  the subject of the formula:

$$v_2 = \sqrt{\frac{2\left(\frac{P_1 - P_2}{\rho} - gh\right)}{1 + f \frac{L}{d}}}$$

- Does this appear correct?
- What am I missing here?
- Why does  $P_{atm}$  not come into it, should I include it ( $P_1$  and  $P_2$  are larger than  $P_{atm}$ )?