



Darcy - Weisbach Equation for Pressure Loss over a Length of Pipe :

$$\Delta P_{friction} = f \frac{L}{D} \frac{\rho v^2}{2}$$

$\Delta P_{friction}$ - Pressure Drop over Pipe [Pa]

$f = \lambda$ - Friction Factor

L - Length of Pipe [m]

D - Hydraulic Diameter of Pipe [m] $D = 2r$ for a circular c/s

ρ - Density of Fluid [kg/m³]

v - Average Velocity of Fluid Flow [m/s]

Bernoulli's Equation :

$$P + \frac{1}{2} \rho v^2 + \rho gh = \text{Constant}$$

P - Pressure [Pa]

ρ - Density of Fluid [kg/m³]

v - Average Velocity of Fluid Flow [m/s]

g - Gravitational Acceleration $g = 9,81$ [m/s²]

h - Height above or below Mean [m]

The valve is opened rapidly.

So putting the two equations together for this problem:

$$P_1 + \frac{1}{2} \rho v_1^2 + \rho g h_1 = P_2 + \frac{1}{2} \rho v_2^2 + \rho g h_2 + \Delta P_{friction}$$

Assuming densities are the same and that h_2 is on the reference line, $h_1 = -h$, and that v_1 is negligible compared to v_2 (large container, small pipe area) and rearranging:

$$P_1 - P_2 - \rho g h = \frac{1}{2} \rho v_2^2 + f \frac{L}{D} \frac{\rho v_2^2}{2}$$

$D = d$ in this example.

Making v_2 the subject of the formula:

$$v_2 = \sqrt{\frac{2 \left(\frac{P_1 - P_2}{\rho} - g h \right)}{1 + f \frac{L}{d}}}$$

- Does this appear correct?
- What am I missing here?
- Why does P_{atm} not come into it, should I include it (P_1 and P_2 are larger than P_{atm})?