

Assume switch a has been open, and b closed for a very long time. Then at time $t=0$, switch a closes and b opens.

We will solve for the inductor current i_L (going from top to bottom) in two ways:

a. Norton equivalent:

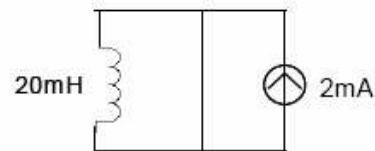
(1) Draw a Norton equivalent for the circuit before time $t=0$ and find the value of $i_L(0^-)$.

Before $t=0$, a is open and b is closed.

Regard the inductor as a load,

$$R_{th} = 6k \parallel 0 = 0$$

$$I_{sc} = 2mA$$



[2 points]

(2) Draw a Norton equivalent for the circuit after time $t=0$ and use this to solve for $i_L(t)$ for $t>0$. (Notice that we could not just draw one Norton equivalent for all times, because we can't include the switches.)

After $t=0$, a is closed and b is open.

To get R_{th} , the current source is treated as an open circuit and the voltage source is treated as a short circuit



$$R_{th} = 6k \parallel 3k = 2k$$

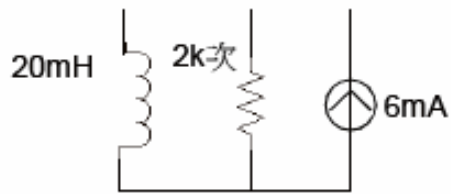
Apply KCL to the node of V_x ,

$$\frac{12 - V_x}{3k} + 2mA = \frac{V_x}{6k} \Rightarrow$$

$$V_x = 12V = V_{oc} = V_{th}$$

$$I_{sc} = \frac{V_{oc}}{R_{th}} = 6mA$$

and Norton equivalent circuit is shown below.



[2 points]

Apply KVL,

$$L \frac{di_L}{dt} = i_R R = (6mA - i_L) 2k \quad (2)$$

Solve this differential equation and we get,

$$i_L(t) = 6mA - (6mA - I_0) \exp(-100000t) \quad [3 \text{ points}]$$

Note for this case, the initial current, I_0 , through the inductor could be arbitrary between 0 and 2mA.