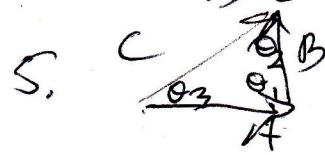


P. 460 1, 5, 13, 17 a, b

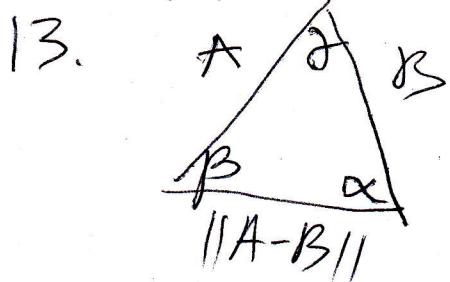
$$1. t = \frac{A \cdot B}{B \cdot B} = \frac{1+4+6}{1+4+4} = \frac{11}{9}, tB = \left(\frac{1}{9}, \frac{2}{9}, \frac{2}{9} \right)$$



$$\cos \theta_1 = \frac{A \cdot B}{\|A\| \|B\|} = \frac{2+3-5}{\sqrt{6} \sqrt{35}} = 0$$

$$\begin{aligned}\|A\| &= \sqrt{6} \\ \|B\| &= \sqrt{35} \\ \|C\| &= \sqrt{41}\end{aligned}$$

$$\cos \theta_2 = \frac{B \cdot C}{\|B\| \|C\|} = \frac{3+12+20}{\sqrt{35} \sqrt{41}} = \boxed{\frac{\sqrt{35}}{\sqrt{41}}}, \quad \cos \theta_3 = \frac{A \cdot C}{\|A\| \|C\|} = \frac{6+4-4}{\sqrt{6} \sqrt{41}} = \boxed{\frac{\sqrt{6}}{\sqrt{41}}}$$



$$\|A-B\|^2 = \|A\| \|A-B\| \cos \beta + \|B\| \|A-B\| \cos \alpha$$

$$\|A\|^2 = \|A\| \|A-B\| \cos \beta + \|A\| \|B\| \cos \gamma$$

$$\|B\|^2 = \|B\| \|A-B\| \cos \alpha + \|B\| \|A\| \cos \beta$$

$$\|A\|^2 + \|B\|^2 = \|A\| \|A-B\| \cos \beta + 2 \|A\| \|B\| \cos \gamma + \|B\| \|A-B\| \cos \alpha$$

$$12. a) \|A\| > 0; \text{ if } A \neq 0, \|A\| = \sum_{k=1}^n |a_{kk}| > 0, \text{ since } A \text{ does not equal zero vector and absolute value of at least one component } > 0$$

if $A=0$, $a_1=0, a_2=0 \dots a_n=0$ st $\|A\|=0$

$$\sum_{k=1}^n |c_{kk}| = |c| \sum_{k=1}^n |a_{kk}| = |c| \|A\|$$

$$\text{Thm 12.5 } \|A+B\|^2 \leq (\|A\| + \|B\|)^2, \quad \sum_{k=1}^n |a_{kk}+b_{kk}|^2 \leq \left(\sum_{k=1}^n |a_{kk}| + \sum_{k=1}^n |b_{kk}| \right)^2$$

$$\sum_{k=1}^n |a_{kk}|^2 + 2 \sum_{k=1}^n |a_{kk}b_{kk}| + \sum_{k=1}^n |b_{kk}|^2 \leq \sum_{k=1}^n |a_{kk}|^2 + 2 \sum_{k=1}^n |a_{kk}| \sum_{k=1}^n |b_{kk}| + \sum_{k=1}^n |b_{kk}|^2$$

$$\sum_{k=1}^n |a_{kk}b_{kk}| \leq \sum_{k=1}^n |a_{kk}| \sum_{k=1}^n |b_{kk}|$$