

**1.11** Let  $Q$  be the operator of an observable and let  $|\psi\rangle$  be the state of our system.

- a.** What are the physical interpretations of  $\langle\psi|Q|\psi\rangle$  and  $|\langle q_n|\psi\rangle|^2$ , where  $|q_n\rangle$  is the  $n^{\text{th}}$  eigenket of the observable  $Q$  and  $q_n$  is the corresponding eigenvalue?
- b.** What is the operator  $\sum_n |q_n\rangle\langle q_n|$ , where the sum is over all eigenkets of  $Q$ ? What is the operator  $\sum_n q_n |q_n\rangle\langle q_n|$ ?
- c.** If  $u_n(x)$  is the wavefunction of the state  $|q_n\rangle$ , write down an integral that evaluates to  $\langle q_n|\psi\rangle$ .