

In Peskin Schroeder from formula 5.87 which is

$$\frac{1}{4} \sum M^2 = 2e^4 \left[ \frac{pk}{pk} + \frac{pk}{pk} + 2m^2 \left( \frac{1}{pk} - \frac{1}{pk} \right) + m^4 \left( \frac{1}{pk} - \frac{1}{pk} \right)^2 \right]$$

they go to formula 5.91:

$$\frac{d\sigma}{d\cos\theta} = \frac{\pi\alpha^2}{m^2} \left( \frac{\dot{\omega}}{\omega} \right)^2 \left[ \frac{\dot{\omega}}{\omega} + \frac{\omega}{\dot{\omega}} - \sin^2\theta \right].$$

From that step it seems to me that  $2m^2 \left( \frac{1}{pk} - \frac{1}{pk} \right) + m^4 \left( \frac{1}{pk} - \frac{1}{pk} \right)^2$  is

somehow equivalent to  $-\sin^2\theta$ .

I saw in other books and there  $-\sin^2\theta$  is related to sum over photon polarizations...so if in Peskin Schroeder

from  $2m^2 \left( \frac{1}{pk} - \frac{1}{pk} \right) + m^4 \left( \frac{1}{pk} - \frac{1}{pk} \right)^2$  they go to  $-\sin^2\theta$  does it mean that

$2m^2 \left( \frac{1}{pk} - \frac{1}{pk} \right) + m^4 \left( \frac{1}{pk} - \frac{1}{pk} \right)^2$  is related to this photon polarization?

I don't understand why exactly  $2m^2 \left( \frac{1}{pk} - \frac{1}{pk} \right) + m^4 \left( \frac{1}{pk} - \frac{1}{pk} \right)^2$  expression has been rewritten into  $-\sin^2\theta$ ?