

In Peskin Schroeder from formula 5.87 which is

$$\frac{1}{4} \sum M^2 = 2e^4 \left[\frac{p\dot{k}}{pk} + \frac{p\dot{k}}{p\dot{k}} + 2m^2 \left(\frac{1}{pk} - \frac{1}{p\dot{k}} \right) + m^4 \left(\frac{1}{pk} - \frac{1}{p\dot{k}} \right)^2 \right]$$

they go to formula 5.91:

$$\frac{d\sigma}{d\cos\theta} = \frac{\pi\alpha^2}{m^2} \left(\frac{\dot{\omega}}{\omega} \right)^2 \left[\frac{\dot{\omega}}{\omega} + \frac{\omega}{\dot{\omega}} - \sin^2\theta \right].$$

From that step it seems to me that $2m^2 \left(\frac{1}{pk} - \frac{1}{p\dot{k}} \right) + m^4 \left(\frac{1}{pk} - \frac{1}{p\dot{k}} \right)^2$ is

somehow equivalent to $-\sin^2\theta$.

I saw in other books and there $-\sin^2\theta$ is related to sum over photon polarizations...so if in Peskin Schroeder

from $2m^2 \left(\frac{1}{pk} - \frac{1}{p\dot{k}} \right) + m^4 \left(\frac{1}{pk} - \frac{1}{p\dot{k}} \right)^2$ they go to $-\sin^2\theta$ does it mean that $2m^2 \left(\frac{1}{pk} - \frac{1}{p\dot{k}} \right) + m^4 \left(\frac{1}{pk} - \frac{1}{p\dot{k}} \right)^2$ is related to this photon polarization?

I don't understand why exactly $2m^2 \left(\frac{1}{pk} - \frac{1}{p\dot{k}} \right) + m^4 \left(\frac{1}{pk} - \frac{1}{p\dot{k}} \right)^2$ expression has been rewritten into $-\sin^2\theta$?