

Kinematic Equations

$$\mathbf{v}_P = \mathbf{v}_A + \boldsymbol{\Omega} \times \mathbf{r}_{P/A} + (\mathbf{v}_{P/A})_{xyz}$$

$$\mathbf{a}_P = \mathbf{a}_A + \dot{\boldsymbol{\Omega}} \times \mathbf{r}_{P/A} + \boldsymbol{\Omega} \times (\boldsymbol{\Omega} \times \mathbf{r}_{P/A}) + 2\boldsymbol{\Omega} \times (\mathbf{v}_{P/A})_{xyz} + (\mathbf{a}_{P/A})_{xyz}$$

| Motion of Moving Reference | Motion of P with respect to moving reference |
|--|--|
| $\mathbf{v}_A = 0$ | $\mathbf{r}_{P/A} = \sqrt{1.25^2 + 2.25^2 - 2(1.25)(2.5) \cos(180 - \theta)} \mathbf{i}$ |
| $\mathbf{a}_A = 0$ | $(\mathbf{v}_{P/A})_{xyz} = (\mathbf{v}_{P/A})_{xyz} \mathbf{i}$ |
| $\boldsymbol{\Omega} = \omega_{AE} \mathbf{k}$ | $(\mathbf{a}_{P/A})_{xyz} = (\mathbf{a}_{P/A})_{xyz} \mathbf{i}$ |
| $\dot{\boldsymbol{\Omega}} = \alpha_{AE} \mathbf{k}$ | |

Motion of slider block P

$$\mathbf{r}_{P/B} = (1.25 \cos \theta \mathbf{i} + 1.25 \sin \theta \mathbf{j})$$

$$\mathbf{v}_P = \boldsymbol{\omega}_{BP} \times \mathbf{r}_{P/B} = (6\mathbf{k}) \times (1.25 \cos \theta \mathbf{i} + 1.25 \sin \theta \mathbf{j}) = (-7.5 \sin \theta \mathbf{i} + 7.5 \cos \theta \mathbf{j})$$

$$\mathbf{a}_{BP} = 0 \text{ (constant } \boldsymbol{\omega}_{BP})$$

$$\mathbf{a}_P = \mathbf{a}_{BP} \times \mathbf{r}_{P/B} - (\omega_{BP}^2)(\mathbf{r}_{P/B})$$

$$\mathbf{a}_P = 0\mathbf{k} \times (1.25 \cos \theta \mathbf{i} + 1.25 \sin \theta \mathbf{j}) - 6^2(1.25 \cos \theta \mathbf{i} + 1.25 \sin \theta \mathbf{j})$$

$$\mathbf{a}_P = (-45 \cos \theta \mathbf{i} - 45 \sin \theta \mathbf{j})$$

Solving for $(\mathbf{v}_{P/A})_{xyz}$ and ω_{AE}

$$\mathbf{v}_P = \mathbf{v}_A + \boldsymbol{\Omega} \times \mathbf{r}_{P/A} + (\mathbf{v}_{P/A})_{xyz}$$

$$(-7.5 \sin \theta \mathbf{i} + 7.5 \cos \theta \mathbf{j}) = 0 + \omega_{AE} \mathbf{k} \times \sqrt{1.25^2 + 2.25^2 - 2(1.25)(2.5) \cos(180 - \theta)} \mathbf{i} + (\mathbf{v}_{P/A})_{xyz} \mathbf{i}$$

$$(-7.5 \sin \theta \mathbf{i} + 7.5 \cos \theta \mathbf{j}) = \omega_{AE} \sqrt{1.25^2 + 2.25^2 - 2(1.25)(2.5) \cos(180 - \theta)} \mathbf{j} + (\mathbf{v}_{P/A})_{xyz} \mathbf{i}$$

$$(\mathbf{v}_{P/A})_{xyz} = -7.5 \sin \theta$$

$$\omega_{AE} = (7.5 \cos \theta) / \sqrt{7.8125 - 6.25 \cos(180 - \theta)} \text{ counterclockwise}$$

Solving for $(\mathbf{a}_{P/A})_{xyz}$ and α_{AE}

$$\mathbf{a}_P = \mathbf{a}_A + \dot{\boldsymbol{\Omega}} \times \mathbf{r}_{P/A} + \boldsymbol{\Omega} \times (\boldsymbol{\Omega} \times \mathbf{r}_{P/A}) + 2\boldsymbol{\Omega} \times (\mathbf{v}_{P/A})_{xyz} + (\mathbf{a}_{P/A})_{xyz}$$

$$\begin{aligned}
(-45\cos\theta \mathbf{i} - 45\sin\theta \mathbf{j}) &= 0 + \alpha_{AE} \mathbf{k} \times \sqrt{7.8125 - 6.25\cos(180 - \theta)} \mathbf{i} + \\
&\quad [(7.5\cos\theta)/\sqrt{7.8125 - 6.25\cos(180 - \theta)}] \mathbf{k} \times \\
&\quad [(7.5\cos\theta)/\sqrt{7.8125 - 6.25\cos(180 - \theta)}] \mathbf{k} \times \sqrt{7.8125 - 6.25\cos(180 - \theta)} \mathbf{i}] \\
&\quad + 2 [(7.5\cos\theta)/\sqrt{7.8125 - 6.25\cos(180 - \theta)}] \mathbf{k} \times -7.5\sin\theta \mathbf{i} + (a_{P/A})_{xyz} \mathbf{i}
\end{aligned}$$

$$\begin{aligned}
(-45\cos\theta \mathbf{i} - 45\sin\theta \mathbf{j}) &= \alpha_{AE} \sqrt{7.8125 - 6.25\cos(180 - \theta)} \mathbf{j} \\
&\quad - (56.25 (\cos\theta)^2 / \sqrt{7.8125 - 6.25\cos(180 - \theta)}) \mathbf{i} \\
&\quad - (112.5 \cos\theta \sin\theta) / \sqrt{7.8125 - 6.25\cos(180 - \theta)} \mathbf{j} + (a_{P/A})_{xyz} \mathbf{i}
\end{aligned}$$

$$(a_{P/A})_{xyz} = (56.25 (\cos\theta)^2 / \sqrt{7.8125 - 6.25\cos(180 - \theta)}) - 45\cos\theta$$

$$\alpha_{AE} = [(-45\sin\theta) / \sqrt{7.8125 - 6.25\cos(180 - \theta)}] + [(112.5 \cos\theta \sin\theta) / (7.8125 - 6.25\cos(180 - \theta))]$$