

$$(a+bt) \frac{dq}{dt} + \frac{1}{c} q = V$$

$$\frac{dq}{dt} + \frac{1}{rc} q = \frac{V}{R}$$

$$\begin{aligned} \mu(t) &= e^{\int \frac{1}{rc} dt} = e^{\int \frac{1}{(a+bt)c} dt} \\ &= e^{\frac{1}{c} \int \frac{1}{b} \frac{1}{u} du} = e^{\frac{1}{bc} \ln|u|} \\ &= e^{\frac{1}{bc} \ln|a+bt|} \\ &= e^{\frac{1}{bc} \ln|a+bt|} = (a+bt)^{\frac{1}{bc}} \end{aligned}$$

$$\frac{d}{dt}((a+bt)^{\frac{1}{bc}} q) = \frac{V}{a+bt} (a+bt)^{\frac{1}{bc}}$$

$$(a+bt)^{\frac{1}{bc}} q = V \left(\int \frac{(a+bt)^{\frac{1}{bc}}}{a+bt} dt \right) + C$$

$$q(0) = q_0$$

$$a^{\frac{1}{bc}} q_0 = V \left(\int \frac{a^{\frac{1}{bc}}}{a} dt \right) + C$$

$$C = a^{\frac{1}{bc}} q_0 - V \left(\int \frac{a^{\frac{1}{bc}}}{a} dt \right), \text{ so}$$

$$q(t) = \frac{V \left(\int \frac{(a+bt)^{\frac{1}{bc}}}{a+bt} dt \right) + a^{\frac{1}{bc}} q_0 - V \left(\int \frac{a^{\frac{1}{bc}}}{a} dt \right)}{(a+bt)^{\frac{1}{bc}}}$$