

$$(A \cup B) \Delta C = (A \Delta C) \Delta (B \setminus A)$$

$$1. [(A \cup C) \setminus (A \cap C)] \Delta (B \setminus A)$$

def of symmetric difference

$$2. [[(A \cup C) \setminus (A \cap C)] \cup (B \setminus A)] \setminus [[(A \cup C) \setminus (A \cap C)] \cap (B \setminus A)]$$

def of symmetric difference

$$3. [[(A \cup C) \cap (A \cup C)] \cup (B \cap A)] \setminus [[(A \cup C) \cap (A \cup C)] \cap (B \cap A)]$$

def of difference and DeMorgans

$$4. [[(A \cup C) \cap (A \cup C)] \cup (B \cap A)] \cap [[(A \cap C) \cup (A \cap C)] \cup (B \cup A)]$$

def of difference and DeMorgans

inorder to reduce number of steps I will use substitution

$$R = (A \cup C), S = (A \cup C), T = (B \cap A)$$

$$5. [(R \cap S) \cup T] \cap [(R \cup S) \cup T]$$

substitution

$$6. [[(R \cap S) \cup T] \cap (R \cup S)] \cup [(R \cap S) \cup T] \cap T]$$

distributive law

$$7. [[(R \cap S) \cap (R \cup S)] \cup [T \cap (R \cup S)]] \cup [[(R \cap S) \cap T] \cup [T \cap T]]$$

distributive law

$$8. [[\emptyset] \cup [T \cap (R \cup S)]] \cup [[(R \cap S) \cap T] \cup [\emptyset]]$$

complement law

$$9. [T \cap (R \cup S)] \cup [(R \cap S) \cap T]$$

identity law

$$10. [(T \cap R) \cup (T \cap S)] \cup [(R \cap S) \cap T]$$

distributive law

$$11. [(B \cap A) \cap (A \cap C)] \cup [(B \cap A) \cap (A \cap C)] \cup [(A \cup C) \cap (A \cup C) \cap (B \cup A)]$$

substitution

$$12. [(B \cap A \cap C)] \cup [(B \cap A) \cap (A \cap C)] \cup [(A \cup C) \cap (A \cup C) \cap (B \cup A)]$$

idempotent

$$13. [(B \cap A \cap C)] \cup [(B \cap \emptyset \cap C)] \cup [(A \cup C) \cap (A \cup C) \cap (B \cup A)]$$

complement

$$14. [(B \cap A \cap C)] \cup \emptyset] \cup [(A \cup C) \cap (A \cup C) \cap (B \cup A)]$$

domination

$$15. [(B \cap A \cap C)] \cup [(A \cup C) \cap (A \cup C) \cap (B \cup A)]$$

identity

$$16. [(B \cap A \cap C)] \cup [((A \cap (A \cup C)) \cup (C \cap (A \cup C))) \cap (B \cup A)]$$

distributive

$$17. [(B \cap A \cap C)] \cup [((A \cap A) \cup (A \cap C)) \cup ((C \cap A) \cup (C \cap C))] \cap (B \cup A)]$$

distributive

$$18. [(B \cap A \cap C)] \cup [(\emptyset \cup (A \cap C)) \cup ((C \cap A) \cup \emptyset)] \cap (B \cup A)]$$

complement

$$19. [(B \cap A \cap C)] \cup [((A \cap C) \cup ((C \cap A))) \cap (B \cup A)]$$

domination