

Multilinear functions.

Let  $V_1$  and  $V_2$  and  $W$  be vector spaces. A map  $f: V_1 \times V_2 \rightarrow W$  is called bilinear etc

Suppose that  $\tau \in V^*$  and  $\theta \in W^*$ ; that is  $\tau$  and  $\theta$  are linear real-valued functions on  $V$  and  $W$ , respectively. Then we obtain a bilinear real-valued Function

$$\tau \otimes \theta: V \times W \rightarrow R$$

by the formula

$$\tau \otimes \theta(v, w) = (\tau v)(\theta w)$$

This bilinear function is called the tensor product of  $\tau$  and  $\theta$ .