

Solution

First, calculate the second moment of area about the neutral axis:

$$I_{\text{NA}} = \frac{bd^3}{12} \quad \text{where } b = 50 \text{ mm and } d = 150 \text{ mm}$$

$$= \frac{50 \times 150^3}{12} \text{ mm}^4$$

$$= \frac{50 \times 150^3}{12} \times 10^{-12} \text{ m}^4$$

$$I_{\text{NA}} = 1.406 \times 10^{-5} \text{ m}^4$$

$$y = 75 \text{ mm} = 75 \times 10^{-3} \text{ m}$$

$$\frac{M}{I} = \frac{\sigma}{y}$$

$$\therefore \sigma = \frac{My}{I}$$

$$\sigma = \frac{720 \times 75 \times 10^{-3}}{1.406 \times 10^{-5}}$$

$$= 3.84 \times 10^6 \text{ N m}^{-2}$$

$$\therefore \text{maximum stress} = 3.84 \text{ MN m}^{-2}$$

Since both edges are equal distances from the neutral axis, then the bottom edge will have a tensile stress of 3.84 MN m^{-2} and the top edge will have a compressive stress of 3.84 MN m^{-2} . Hence, the stress in the beam varies uniformly across the section from 3.84 MN m^{-2} (compressive) at the top to 3.84 MN m^{-2} (tensile) at the bottom. This variation is often represented in the