

$$\begin{aligned}
& \text{with}(\text{VectorCalculus}) : \\
& n := \langle -\sin(\theta), \cos(\theta) \rangle \\
& \qquad n := -\sin(\theta)e_x + (\cos(\theta))e_y \tag{1} \\
& ee := \langle \cos(\theta), \sin(\theta) \rangle \\
& \qquad ee := (\cos(\theta))e_x + (\sin(\theta))e_y \tag{2} \\
& gg := -g \cdot n \\
& \qquad gg := (g \sin(\theta))e_x - g \cos(\theta)e_y \tag{3} \\
& RR := R \cdot n \\
& \qquad RR := -R \sin(\theta)e_x + (R \cos(\theta))e_y \tag{4} \\
& aaM := aM \cdot ee \\
& \qquad aaM := (aM \cos(\theta))e_x + (aM \sin(\theta))e_y \tag{5} \\
& am := aaM + \langle w, 0 \rangle \\
& \qquad am := (aM \cos(\theta) + w)e_x + (aM \sin(\theta))e_y \tag{6} \\
& NN := \langle 0, N \rangle \\
& \qquad NN := (N)e_y \tag{7} \\
& eq1 := m \cdot am - NN - m \cdot gg \\
& \qquad eq1 := (m(aM \cos(\theta) + w) - m g \sin(\theta))e_x + (m aM \sin(\theta) - N + m g \cos(\theta))e_y \tag{8} \\
& eq2 := M \cdot aaM + NN - RR - M \cdot gg \\
& eq2 := (M aM \cos(\theta) + R \sin(\theta) - M g \sin(\theta))e_x + (M aM \sin(\theta) + N - R \cos(\theta) \\
& \qquad + M g \cos(\theta))e_y \tag{9} \\
& x1 := m(aM \cos(\theta) + w) - m g \sin(\theta) \\
& \qquad x1 := m(aM \cos(\theta) + w) - m g \sin(\theta) \tag{10} \\
& x2 := m aM \sin(\theta) - N + m g \cos(\theta) \\
& \qquad x2 := m aM \sin(\theta) - N + m g \cos(\theta) \tag{11} \\
& x3 := M aM \cos(\theta) + R \sin(\theta) - M g \sin(\theta) \\
& \qquad x3 := M aM \cos(\theta) + R \sin(\theta) - M g \sin(\theta) \tag{12} \\
& x4 := M aM \sin(\theta) + N - R \cos(\theta) + M g \cos(\theta) \\
& \qquad x4 := M aM \sin(\theta) + N - R \cos(\theta) + M g \cos(\theta) \tag{13} \\
& \text{solve}(\{x1=0, x2=0, x3=0, x4=0\}, [w, aM, R, N]) \\
& \left[\left[w = \frac{g \sin(\theta) (\cos(\theta)^2 m + M \cos(\theta)^2 + m \sin(\theta)^2 + M \sin(\theta)^2)}{M \cos(\theta)^2 + m \sin(\theta)^2 + M \sin(\theta)^2}, aM = \right. \right. \tag{14} \\
& \qquad \left. \left. - \frac{\sin(\theta) m g \cos(\theta)}{M \cos(\theta)^2 + m \sin(\theta)^2 + M \sin(\theta)^2}, R \right] \right]
\end{aligned}$$

$$\begin{aligned}
 &= \frac{M g \left(\cos(\theta)^2 m + M \cos(\theta)^2 + m \sin(\theta)^2 + M \sin(\theta)^2 \right)}{M \cos(\theta)^2 + m \sin(\theta)^2 + M \sin(\theta)^2}, N \\
 &= \frac{m g \cos(\theta) M \left(\cos(\theta)^2 + \sin(\theta)^2 \right)}{M \cos(\theta)^2 + m \sin(\theta)^2 + M \sin(\theta)^2} \Bigg] \\
 &\rightarrow \text{simplify} \left(- \frac{\sin(\theta) m g \cos(\theta)}{M \cos(\theta)^2 + m \sin(\theta)^2 + M \sin(\theta)^2}, \text{trig} \right) \\
 &\quad - \frac{m g \sin(\theta) \cos(\theta)}{m + M - \cos(\theta)^2 m}
 \end{aligned} \tag{15}$$